

UNIT 4: GRAPHING USING INTERCEPTS

I can graph lines in $Ax + By = C$ form using the x and y-intercepts.

Standard Form

Graphing Lines, $Ax + By = C$ with x and y intercepts

Equations that are written in $Ax + By = C$ form are easier to graph using the x-intercept and y-intercepts. Before we begin, let's see what standard form looks like.

What is Standard Form?

$Ax + By = C$

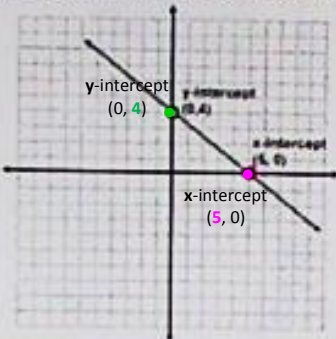
Standard form is presented as

Where A and B are coefficients and C is a constant

- Examples:
- $2x + 4y = 8$
 - $5x - 7y = 12$
 - $3x - 9y = -18$

$$\begin{array}{r|l}
 -3x + 5y = 9 & \begin{array}{l} x/y \\ 0/1/5 \\ -3/0 \end{array} \\
 \hline
 \frac{5y}{5} = \frac{9}{5} & \begin{array}{l} -3x = 9 \\ -3 \quad -3 \\ \hline x = -3 \end{array}
 \end{array}$$

Now let's review what the term **intercepts** means. An intercept is where your line crosses an axis. We have an **x intercept** and a **y intercept**.



The point where the line touches the **x axis** is called the **x intercept**.

The point where the line touches the **y axis** is called the **y intercept**.

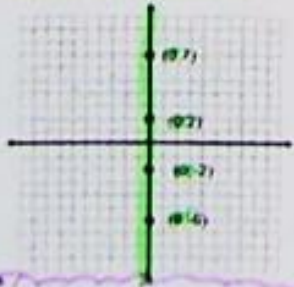


We can find the points where the line crosses the x and y axis, then we would have two points and we'd be able to draw a line.

When equations are written in standard form, it is pretty easy to find the intercepts. Take a look at this diagram, as it will help you to understand the process.

Y Intercept

Any point on the y axis is going to have an x coordinate of 0. Take a look!

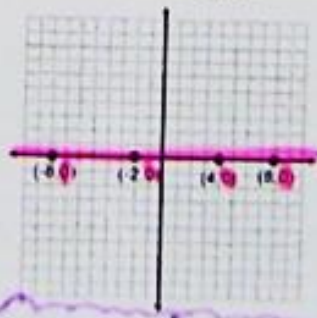


All of these points are y intercepts.

So, to find the y intercept within an equation, we are going to let $x = 0$.

X Intercept

Any point on the x axis is going to have a y coordinate of 0. Take a look!



All of these points are x intercepts.

So, to find the x intercept within an equation, we are going to let $y = 0$.

Now, let's apply this. Just remember

To find the x Intercept: Let $y = 0$

To find the y Intercept: Let $x = 0$

Example 1

$2x + 4y = 8$

Let $y = 0$

$2x + 4y = 8$

$2x + 4(0) = 8$

$2x + 0 = 8$

$\frac{2x}{2} = \frac{8}{2}$

$x = 4$

The x intercept is: $(4, 0)$

Let $x = 0$

$2x + 4y = 8$

$2(0) + 4y = 8$

$0 + 4y = 8$

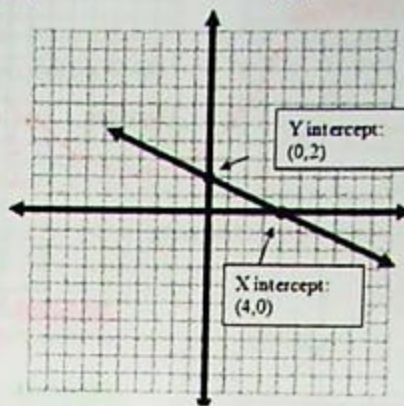
$\frac{4y}{4} = \frac{8}{4}$

$y = 2$

The y intercept is: $(0, 2)$

The x intercept is: $(4, 0)$

The y intercept is: $(0, 2)$



$\frac{6x}{6} = \frac{24}{6}$
 $x = 4$

$\frac{-3y}{-3} = \frac{24}{-3}$
 $y = -8$

$\frac{-2x}{-2} = \frac{-8}{-2}$
 $x = 4$

Use the x and y intercepts to graph the equations.

1) $x + y = -6$

y-intercept: $(0, -6)$ $0 + y = -6$

x-intercept: $(-6, 0)$ $x + 0 = -6$

2) $6x - 3y = 24$

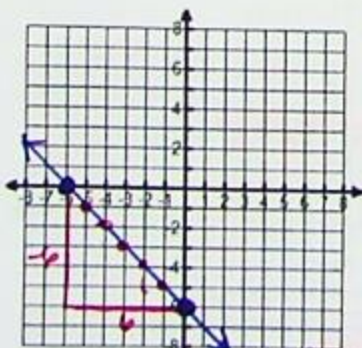
y-intercept: $(0, -8)$

x-intercept: $(4, 0)$

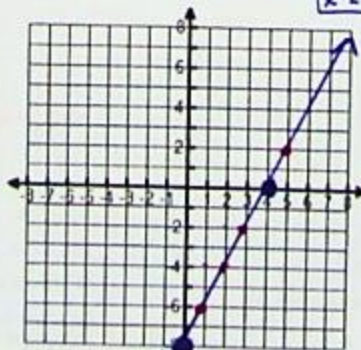
3) $-2x + y = -8$

y-intercept: $(0, -8)$

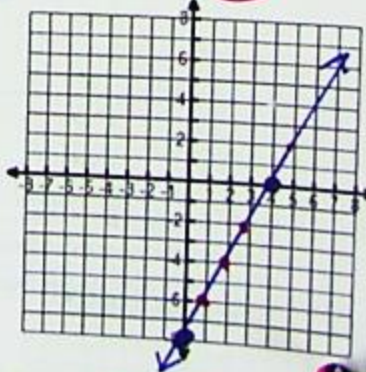
x-intercept: $(4, 0)$



$m = \frac{-6}{6} = -1$
 slope-intercept form
 $y = -x - 6$



$\frac{8}{4} = 2$
 slope-intercept form
 $y = 2x - 8$



Same!
 slope-intercept form
 $y = 2x - 8$

A STRATEGY – to make it even easier!

Look at the equation in problem 1: $x + y = -6$

If x equals zero, place your finger over x and see what y equals!

$y = -6$ $(0, \underline{\quad})$

If y equals zero, place your finger over y to see what x equals!

$x = -6$ $(\underline{\quad}, 0)$

Now you have two points, $(0, -6)$ and $(-6, 0)$. Graph and connect them to see the line they create.

You can use this method even if x or y is multiplied by a number... because any number times zero equals ZERO! That's what the finger tips in problem 2 above are showing!