

UNIT 2: EQUATIONS & INEQUALITIES

Unit 2, Page 35

ONE SOLUTION, NO SOLUTION AND ALL REAL NUMBERS

Objectives: I can solve multi-step equations with variables on both sides with the distributive property and identify equations with no solution or all real numbers.

Examples:

1. $4(2n + 5) = 3n + 10$

$$\begin{array}{r} 8n + (-20) \\ -3n \\ \hline 5n + (-20) \end{array} \quad \begin{array}{r} 3n + 10 \\ +20 \\ \hline 3n + 30 \\ \div 5 \\ \hline 3n + 30 \\ -3n \\ \hline 30 \\ \div 3 \\ \hline 10 \end{array}$$

One solution
 $n=6$

check

$$4[2(6) + (-5)] = 3(6) + 10$$

$$4(12 + (-5)) = 18 + 10$$

$$4(7) = 28$$

$$28 = 28$$

2. $2(4x + 7) - 10 = 3x + 5x$

$$8x + 14 - 10 = 8x$$

$$8x + 4 = 8x$$

$$-8x \quad -8x$$

$4 = 0$ False
No Solution

3. $2(4x + 7) + 2x = 8x + 14$

$$8x + 14 + 2x = 8x + 14$$

$$10x + 14 = 8x + 14$$

$$-8x \quad -8x$$

$$2x + 14 = 14$$

$$-14 \quad -14$$

$$2x = 0$$

$$\frac{2x}{2} = \frac{0}{2}$$

One solution
 $x=0$

If you get a FALSE statement...like $5=2$, then no solution would satisfy the equation...write **NO SOLUTION**

If you get a TRUE statement...like $5=5$, then all real numbers would satisfy the equation...write **ALL REAL #'s**

Practice:

1. $8(k + 3) = 12k - 4$

$$\begin{array}{r} 8k + 24 \\ -8k \\ \hline 24 \\ +4 \\ \hline 28 = \frac{4k}{4} \\ \hline 7 = k \end{array}$$

2. $-3(5 + 9c) = 25 + 27c$

$$\begin{array}{r} -15 + 27c \\ -27c \\ \hline -15 = 25 \\ \hline \text{False} \\ \text{No Solution} \end{array}$$

3. $6x + 5 = 5(3x + 1) - 9x$

$$\begin{array}{r} 6x + 5 \\ -6x \\ \hline 5 = 5x + 5 + (-9x) \\ 5 = 6x + 5 - 9x \\ -6x \quad -6x \\ \hline 5 = 5 \end{array}$$

All Real TRUE Numbers

4. $5 - 11t = 7(5 + 2t)$

$$\begin{array}{r} 5 + 11t \\ +14t \\ \hline 5 + 3t \\ -2 \\ \hline 3t = \frac{30}{3} \\ \hline t = 10 \end{array}$$

5. $-2(18 + 3y) = 7y + 2y$

$$\begin{array}{r} -36 + 6y \\ -6y \\ \hline -36 = 9y \\ -6y \\ \hline -36 = 3y \\ \div 3 \\ \hline -12 = y \end{array}$$

6. $2(4a + 12) = 6a + 1$

$$\begin{array}{r} 8a + (-24) \\ -6a \\ \hline 2a + (-24) \\ +24 \\ \hline 2a = \frac{1}{2} \\ \div 2 \\ \hline a = \frac{25}{2} \text{ or } 12.5 \end{array}$$