

UNIT 1: SIMPLIFY EXPRESSIONS

Objectives: I can identify types of rational numbers and express equivalent numbers for comparison.

Notes

Rational Numbers

Numbers have different classifications. Some numbers can be classified in multiple ways. A rational number is any number that you can write as a ratio, $\frac{a}{b}$, of two integers, where b is not zero. The diagram below shows relationships among rational numbers.

can write as a fraction

Divide by zero?

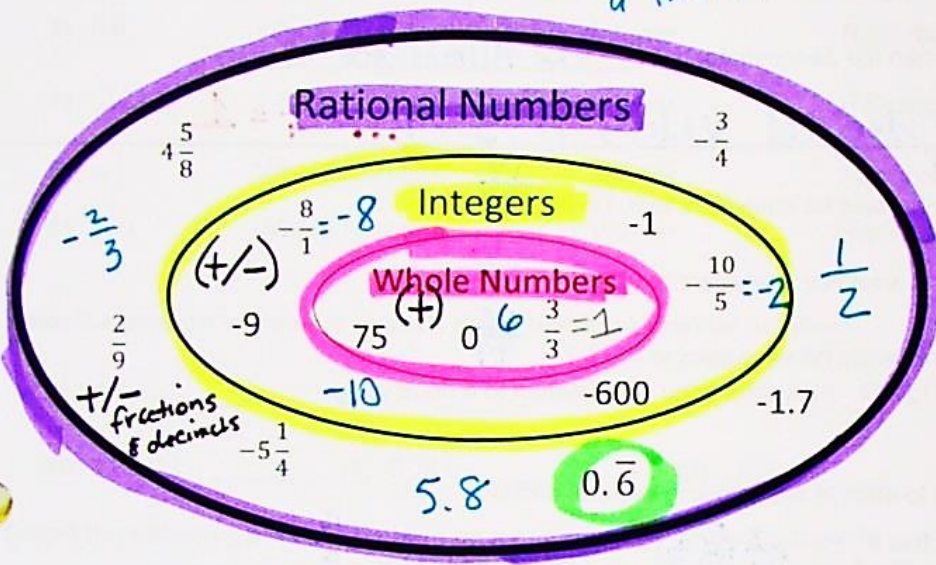
$$\frac{N}{0} \leftarrow \text{No!}$$

Divide by something else?

$$\frac{0}{K} \leftarrow \text{OK}$$

$$\begin{array}{r} 6 \\ 3 \overline{)6} \\ \underline{6} \\ 0 \end{array}$$

error!



Always simplify numbers before classifying them. Every whole number is also an integer and a rational number. Every integer is also a rational number.

Practice

Identify the classification(s) for the following numbers by circling the classification(s) for each.

- 1) 5.8 $5\frac{8}{10} \rightarrow 5\frac{4}{5} \rightarrow \frac{29}{5}$ Whole Number Integer Rational Number
- 2) 6 Whole Number Integer Rational Number
- 3) -10 Whole Number Integer Rational Number
- 4) $0.\overline{6} = \frac{6}{9} = \frac{2}{3}$ Whole Number Integer Rational Number
- 5) $\frac{1}{2}$ Whole Number Integer Rational Number
- 6) $-\frac{2}{3}$ Whole Number Integer Rational Number

a negative on a fraction doesn't make it an integer ... only if you can simplify it to get an integer Ex $-\frac{15}{3} = -5$

Express each of the fractions as decimals.

1) $\frac{1}{9} = \underline{0.\overline{1}}$

2) $\frac{2}{9} = \underline{0.\overline{2}}$

3) $\frac{3}{9} = \underline{0.\overline{3}}$

4) $\frac{4}{9} = \underline{0.\overline{4}}$

5) $\frac{5}{9} = \underline{0.\overline{5}}$

6) $\frac{6}{9} = \underline{0.\overline{6}}$

7) $\frac{7}{9} = \underline{0.\overline{7}}$

8) $\frac{8}{9} = \underline{0.\overline{8}}$

9) $\frac{9}{9} = \underline{1}$

10) What pattern is shown when the denominator is 9? the numerator is

the repeating decimal unless it's 9... $\frac{9}{9} = 1$

11) What fraction do you think would be equivalent to $0.\overline{14}$? $\frac{14}{99}$

12) What fraction do you think would be equivalent to $0.\overline{128}$? $\frac{128}{999}$

13) What fraction do you think would be equivalent to $0.\overline{32}$? $\frac{32}{99}$

Check your answers to #11 - 13 by changing your fraction to a decimal.

Write the fraction equivalent to each of the following decimal numbers.

14) $-0.\overline{2} = \underline{-\frac{2}{9}}$

15) $5.\overline{3} = \underline{5\frac{3}{9} = 5\frac{1}{3}}$ (reduced!)

16) $0.444444\overline{4} = \underline{\frac{4}{9}}$

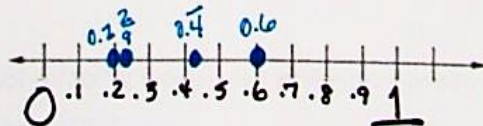
17) $-0.\overline{16} = \underline{-\frac{16}{99}}$

18) $4.\overline{124} = \underline{4\frac{124}{999}}$

19) $0.272727\overline{27} = \underline{\frac{27 \div 9}{99 \div 9} = \frac{3}{11}}$ (1)

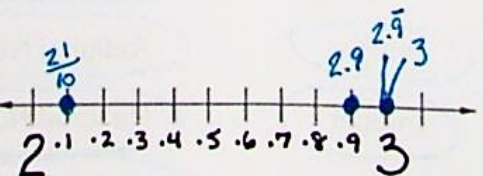
Graph the following sets of numbers on a number line. Then list them in order from least to greatest.

Between 0 and 1
20) $\{0.6, 0.2, \frac{2}{9}, 0.\overline{4}\}$
 \uparrow
 $0.\overline{2}$



0.2 $\frac{2}{9}$ $0.\overline{4}$ 0.6

Between 2 and 3
21) $\{2.9, \frac{21}{10}, 2.\overline{9}, 3\}$
 \uparrow
2.1



$\frac{21}{10}$ 2.9 $2.\overline{9}$ 3

$2.\overline{9} = 2\frac{9}{9} = \underline{3}$